



# Determination of Magnetic Transitions: Effective Spin Models and Monte Carlo Simulations

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“Magnetic Materials from First Principles”, TÜBITAK Workshop  
November 25, 2021, 10:00–10:45 AM and 11:00–11:59 PM TRT

# Scope of magnetic materials in this talk

This talk focuses on **magnetic insulators** with well-localized spins.

3D examples:



2D examples:



# What magnetic properties can we calculate?

Quantity	Requires
Ground-state magnetization $M(0)$	DFT (VASP)
Magnetization curve $M(T)$	+ Monte Carlo
Curie temperature $T_c$	+ Monte Carlo
Paramagnetic susceptibility $\chi(T)$	+ Monte Carlo
Magnetic structure factor $M_s(q)$	+ Monte Carlo
Spin wave dispersions $\omega(q)$	+ Monte Carlo
Hysteresis curve $M(H)$	+ micromagnetics
Coercive field $H_c$	+ micromagnetics

# A Multiscale Modeling Approach

First principles  
(DFT)



Effective spin  
model



Thermodynamic  
properties

$$\hat{H} = \hat{H}_{ee} + \hat{H}_{eN} \\ + \hat{H}_{NN} + \hat{H}_{SO} \\ + \dots \\ \text{eV}$$

$$\hat{H}_{\text{eff}} = - \sum_{\langle ij \rangle} J_{ij} \hat{\mathbf{S}}_i \cdot \hat{\mathbf{S}}_j \\ + \sum_i H_{\text{MAE}}(\hat{\mathbf{S}}_i) + \dots$$

$$M(0) \\ M(T) \\ T_c \\ \dots$$

Energy scales  
1 eV – 10 eV

Energy scales  
1  $\mu\text{eV}$  – 1 eV

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- I supply Jupyter notebooks (Python) and C++ code
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Therefore:

- I show you Mathematica notebooks and C++ code
- You go through examples later on

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We focus on  $\text{CrI}_3$  as a case study!

[Most of this session will be in Mathematica notes]

# Summary: Monolayer CrI<sub>3</sub>

Attempt 1 (nearest neighbor Ising model):	$T_c = 22 \text{ K}$
Attempt 2 (second-neighbor Ising model)	$T_c = 140 \text{ K}$
Attempt 3 (classical Heisenberg model):	$T_c = 0 \text{ K}$
Attempt 4 (classical Heis + easy-axis aniso):	$T_c = 50 \text{ K}$
Attempt 5 (quantum Heis + easy-axis aniso):	???
<b>Experiment:</b>	$T_c = 45 \text{ K}$

There is a large number of papers on this material, both experimental and theoretical, in case you are interested.

# Conclusions (Main Lessons Learned?)

- Magnetism in 2D is subtle and complicated!
- Ferromagnetic order in 2D can exist, but it requires two ingredients:
  - exchange coupling  $J$
  - easy-axis magnetic anisotropy  $K$
- **To make a room-temperature 2D magnetic material, we must optimize both of these properties.**

# Beyond ferromagnetism

## Classical magnetic order

- Antiferromagnetism
- 120-degree (Y) antiferromagnetism
- Non-commensurate states (spin density wave)
- Non-collinear magnetism, e.g., helimagnets
- Classical geometric & disorder frustration

## Quantum magnetism

- Valence bond solid
- Resonating valence bonds
- Valence bond liquid; spin liquid
- Quantum geometric & disorder frustration

Itinerant magnetism ...

Multiferroics ...

## Acknowledgments

- Dr. Deniz Çakır
- Dr. Dilanga Siriwardane
- Dr. Cem Sevik
- Dr. Sevil Sarıkurt

E. M. D. Siriwardane, P. Karki, Y. L. Loh, and D. Çakır, “Engineering magnetic anisotropy and exchange couplings in double transition metal MXenes via surface defects,” [Journal of Physics: Condensed Matter 33, 035801 \(2020\)](#)

E. M. D. Siriwardane, P. Karki, Y. L. Loh, and D. Çakır, “Strain–Spintronics: Modulating Electronic and Magnetic Properties of Hf<sub>2</sub>MnC<sub>2</sub>O<sub>2</sub> MXene by Uniaxial Strain,” [J. Phys. Chem. C 123, 19, 12451-12459 \(2019\)](#)